

**Industrial simulation of fluid flow and fluid-structure interaction with SPH from the VPS software**

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## Introduction

ESI-Group is a world-leading engineering software company

VIRTUAL PRODUCT ENGINEERING

Recent applications involving SPH have been requested for or conducted for:

- Maritime field
- Automotive sector
- Power generation
- Aeronautics
- Other

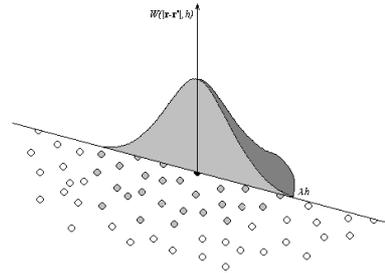
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### Particle Method SPH

- Smoothed Particle Hydrodynamics
- Meshless method for continuum mechanics
- Origins in modelling of cosmic physics
- Significantly enhanced for fluid-flow
- Handles free-surface and other interfaces
- SPH is available for fluid flow and structural dynamics.



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### SPH basic concept

#### ✓ Kernel approximation

$$f(x) = \int f(x')W(x-x',h)dx'$$

$$\nabla f(x) = \int f(x')\nabla W(x-x',h)dx'$$

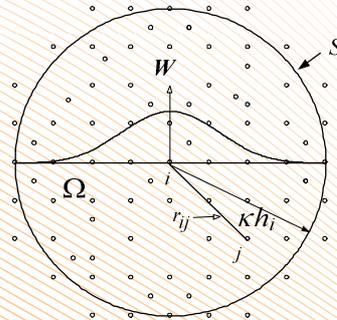
$h$  – Smoothing length

$W$  – Smoothing function

#### ✓ Particle approximation

$$f_i = \sum_{j=1}^N \left( \frac{m_j}{\rho_j} \right) f_j W(x_i - x_j, h)$$

$$\nabla f_i = \sum_{j=1}^N \left( \frac{m_j}{\rho_j} \right) f_j \nabla_i W(x_i - x_j, h)$$



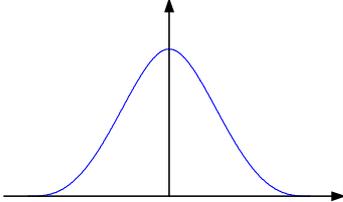
### Properties smoothing function

- ✓ **Normalization:**  

$$\int W(\mathbf{x} - \mathbf{x}', h) d\mathbf{x}' = 1$$
- ✓ **Compactly supported**  

$$W(\mathbf{x} - \mathbf{x}') = 0 \quad |\mathbf{x} - \mathbf{x}'| > \kappa h$$
- ✓ **Delta function property**  

$$\lim_{h \rightarrow 0} W(\mathbf{x} - \mathbf{x}', h) = \delta(\mathbf{x} - \mathbf{x}')$$



**Illustration of a smoothing function**



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### Fluid Flow Equations

- Conservation of Mass
 
$$\frac{d\rho_i}{dt} = \sum_j m_j (\mathbf{v}_i - \mathbf{v}_j) \cdot \nabla_i W_{ij}$$
- Conservation of Momentum
 
$$\frac{d\mathbf{v}_i}{dt} = - \sum_j m_j \left( \frac{p_j}{\rho_j^2} + \frac{p_i}{\rho_i^2} \right) \nabla_i W_{ij}$$
- Conservation of Energy
 
$$\frac{du_i}{dt} = \frac{1}{2} \sum_j m_j \left( \frac{p_i}{\rho_i^2} + \frac{p_j}{\rho_j^2} \right) (\mathbf{v}_i - \mathbf{v}_j) \nabla_i W_{ij}$$
- Equation of State
 
$$p_i = {}^0 p_i + K \left[ \left( \frac{\rho_i}{{}^0 \rho_i} \right)^\gamma - 1 \right]$$



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## Momentum Equations

### Momentum formalism

- the expressions including the pressure to be used in the momentum and energy equations are not unique. The default is:

$$\frac{P_i}{\rho_i^2} + \frac{P_j}{\rho_j^2}$$

The alternative is:

$$\frac{P_i + P_j}{\rho_i \cdot \rho_j}$$

It is better to select this alternative for simulations involving materials with widely different densities but similar pressures i.e. water and air.



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## Treatment of Shocks

Dissipation term:

$$\frac{d\mathbf{v}_i}{dt} = -\sum_j m_j \left( \frac{p_i}{\rho_i^2} + \frac{p_j}{\rho_j^2} + \Pi_{ij} \right) \nabla_i W_{ij}$$

$$\frac{dw_i}{dt} = \frac{1}{2} \sum_j m_j \left( \frac{p_i}{\rho_i^2} + \frac{p_j}{\rho_j^2} + \Pi_{ij} \right) (\mathbf{v}_i - \mathbf{v}_j) \cdot \nabla_i W_{ij}$$

Artificial Viscosity:

$$\Pi_{ij} = \frac{2}{\rho_i + \rho_j} \left( -\alpha \frac{c_i + c_j}{2} \mu_{ij} + \beta \mu_{ij}^2 \right)$$

$$\mu_{ij} = \begin{cases} \frac{1}{2} (h_i + h_j) \frac{(\mathbf{v}_i - \mathbf{v}_j) \cdot (\mathbf{r}_i - \mathbf{r}_j)}{|\mathbf{r}_i - \mathbf{r}_j|^2 + \eta^2} & (\mathbf{v}_i - \mathbf{v}_j) \cdot (\mathbf{r}_i - \mathbf{r}_j) < 0 \\ 0 & (\mathbf{v}_i - \mathbf{v}_j) \cdot (\mathbf{r}_i - \mathbf{r}_j) \geq 0 \end{cases}$$

Artificial viscosity:

- Required to make stable simulation involving pressure waves. For shock type of phenomena, parameter values of 1 to 1.5 are recommended. For (relatively slow) fluid flow simulations, the first parameter may be orders of magnitude smaller.



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### Material with strength (SPH)

- ✓ **Constitutive modeling (Jaumann rate)**

$$\dot{\tau}^{\alpha\beta} - \tau^{\alpha\gamma} R^{\beta\gamma} - \tau^{\gamma\beta} R^{\alpha\gamma} = G\bar{\mathcal{E}}^{\alpha\beta}$$
- ✓ **Strain rate and Rotation rate**

$$\epsilon^{\alpha\beta} = \frac{1}{2} \left( \frac{\partial v^\alpha}{\partial x^\beta} + \frac{\partial v^\beta}{\partial x^\alpha} \right)$$

$$R^{\alpha\beta} = \frac{1}{2} \left( \frac{\partial v^\alpha}{\partial x^\beta} - \frac{\partial v^\beta}{\partial x^\alpha} \right)$$
- ✓ **von Mises flow stress and von Mises rule**

$$J = \sqrt{\tau^{\alpha\beta} \tau^{\alpha\beta}}$$

$$\tau^{\alpha\beta} = \tau^{\alpha\beta} \sqrt{J_0 / 3J^2}$$

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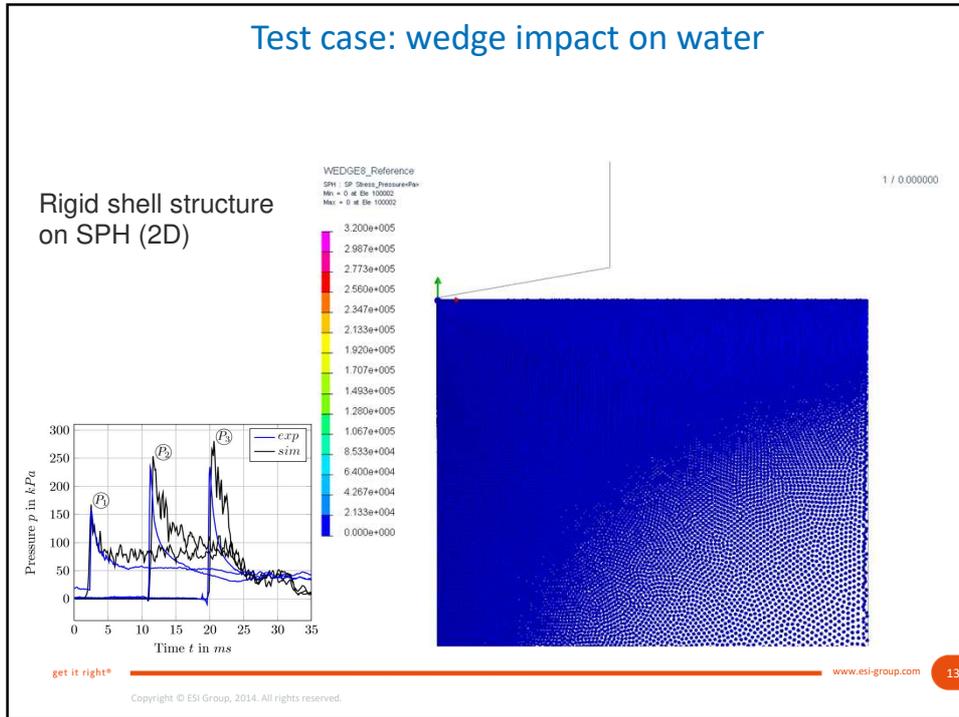
### SPH – Selected features

- The SPH method is fully integrated in the finite element code VPS (explicit version: PAM-CRASH).
- Standard Monaghan formulation incl. deviatoric strength
- Multi-material in SPH
- Pressure correction (similar to delta-SPH)
- Displacement corrections
- Variable smoothing length.
- Symmetry planes & periodic boundaries
- Special filling option (EWVT)
- Material models: JWL(detonation), Hydrodynamic-EP, Johnson-Cook, Murnaghan (Tait) EOS, elastic-plastic with damage, viscous fluids
- Coupling to VPS FE through contact algorithms.

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### Aerospace applications

Assessment of Whipple shield for hyper-velocity impact

The **Whipple shield** hypervelocity impact shield is used to protect spacecraft from collisions with micrometeoroids and orbital debris whose velocities range between 3 and 18 kilometres per second (*Wikipedia*)

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### Aerospace applications

#### Crashworthiness of Aircraft for High Velocity Impact (CRAHVI)



**EADS**

2001-2004

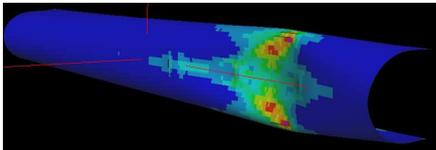
**DLR**

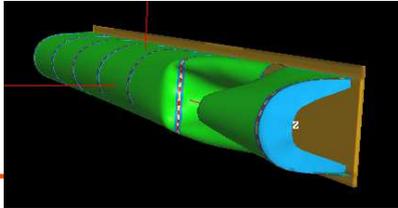


**NLR**



FOD : foreign object damage  
Birdstrike, Hail, Rubber  
SPH validation for bird + water





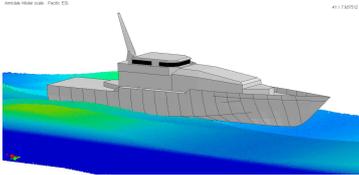
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### Maritime applications

#### Ship Studies – Interaction of Waves and Structures



*Image from <http://www.austal.com/>*



*Image from simulation by Pacific ESI*

Essential to the study of ship behaviours are waves, the ship structures, and their interaction. ESI Group has developed techniques within the VPS software suite to achieve this in a commercially robust package.



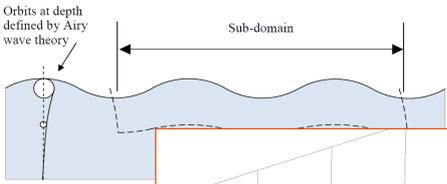
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### Maritime applications

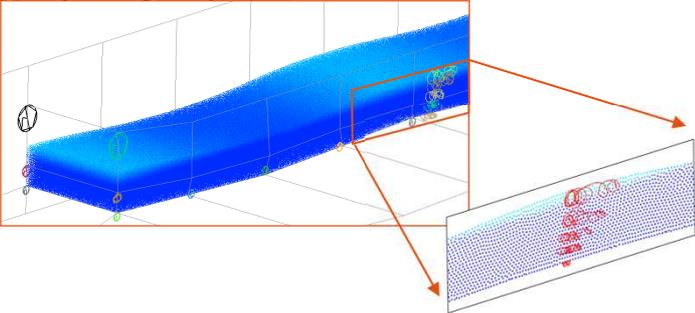
**Regular Wave Development - Moving Floor Pacific** ESI has developed a novel technique to allow continuous waves to be developed, over many wavelengths.



Orbits at depth defined by Airy wave theory

Sub-domain

Trajectories of discrete SPH nodes at various depths indicate the orbital motion is developed with orbits decreasing in diameter with depth, as prescribed by Airy Wave Theory.





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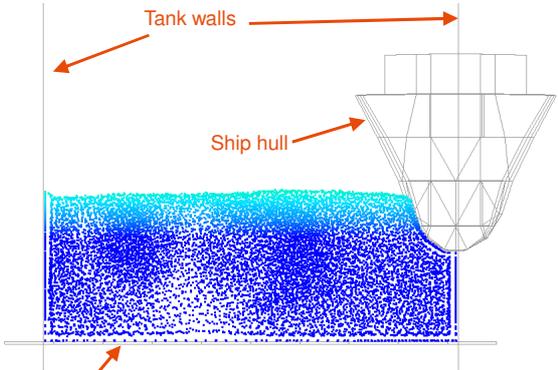
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### Maritime applications

**FE-SPH : Fluid Structure Interaction**

The image at right shows a section through the ship (half model) and the tank.

Industrially robust "Contact Interfaces" are used to keep SPH from passing through shell elements – of the ship and the "tanks".



Tank walls

Ship hull

Moving floor of tank

Section through model



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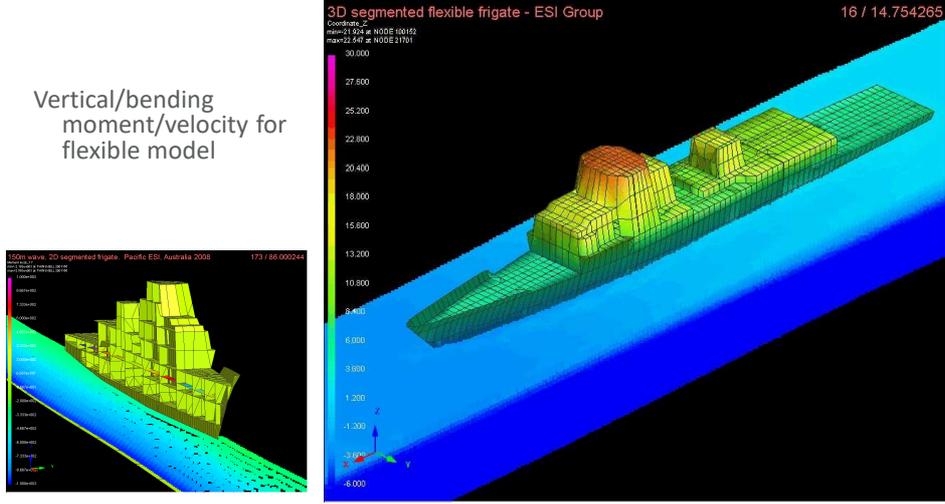
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### Generic Frigate Model

### Fluid dynamics - maritime

Vertical/bending moment/velocity for flexible model



3D segmented flexible frigate - ESI Group 16 / 14.754285

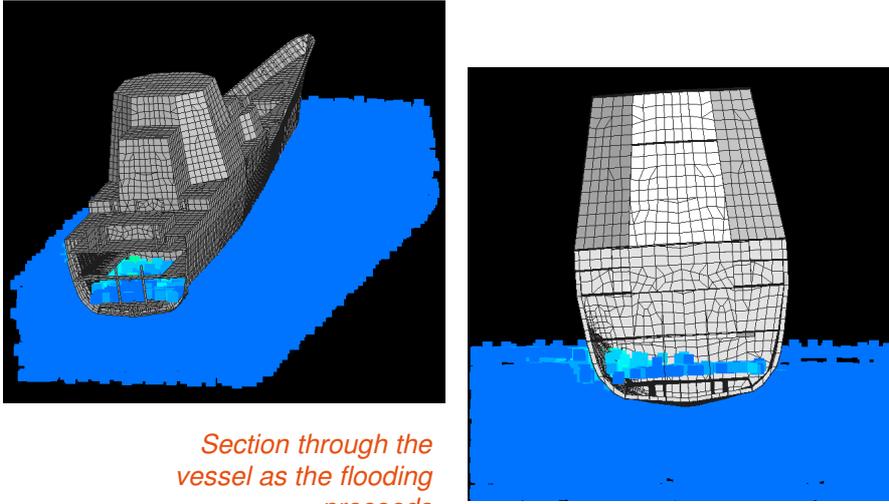
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animation will be at the end of the presentation

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### Fluid dynamics - maritime

### FLOODING



Section through the vessel as the flooding proceeds

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## Tsunami

## Fluid dynamics - maritime

*Animation of Tsunami-like wave entering a building will be the end of the presentation*

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## Offshore applications

### Dynamic Response of Platform in Waves

The platform is tethered with flexible cables; the cranes are also deformable.

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## Offshore applications

### Life Boat Water Entry

- A 'blind' benchmark study was of the impact of a life boat on water, conducted for LB water entry into waves

Figure 1.1: Hit point definition.

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## Offshore applications

### Life Boat Water Entry

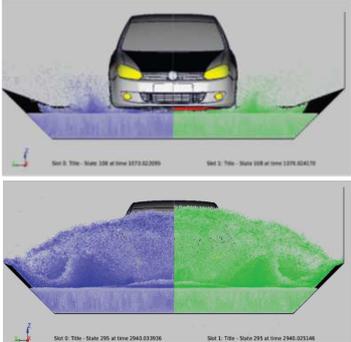
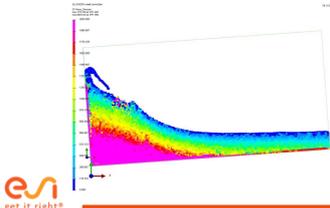
- The (x- and z-) accelerations from the PAM-CRASH simulations at 3 different locations at the hull of the LB have been compared to the results from 3 scale tests.

Hit point : HP3 Wave dir. : Head

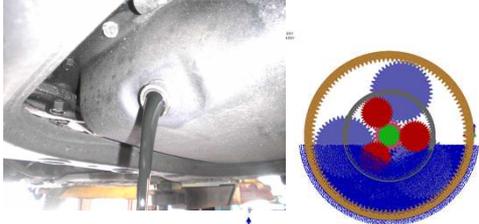
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### Automotive applications

- Applications in which SPH comprise:
- Airbag inflation (not by SPH but by FPM)
- Water management
- Sloshing in fuel tanks
- Oil flow in bearings and oil churning
- dipping into the paint tank

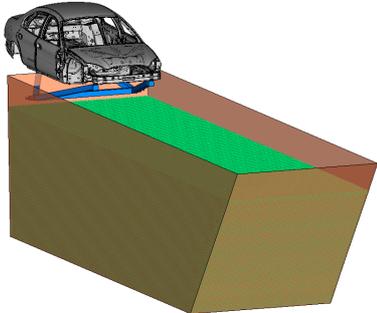


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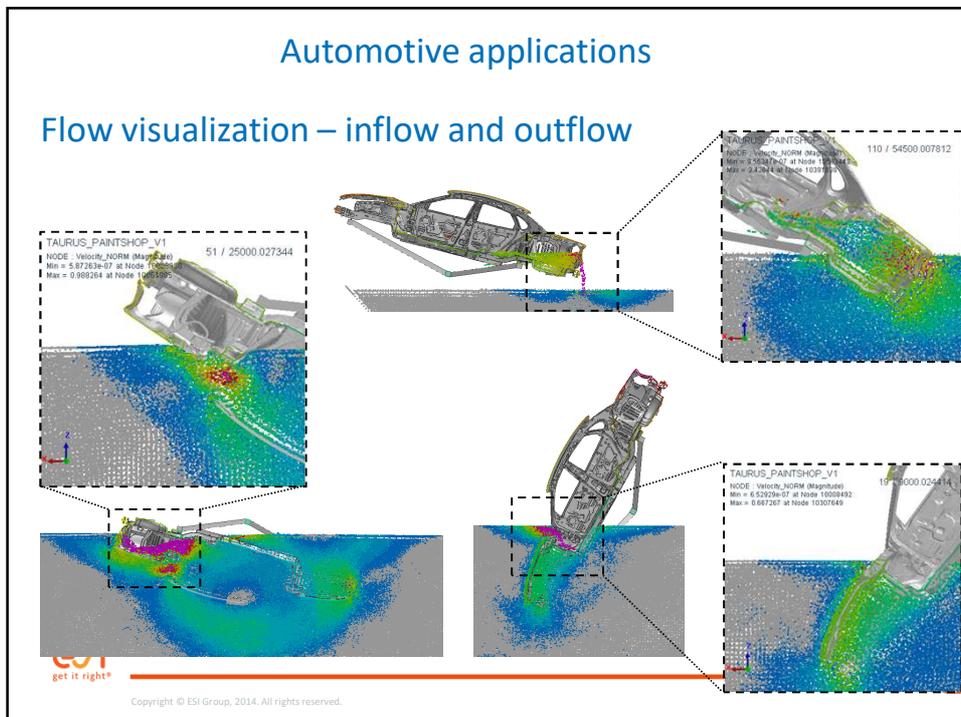
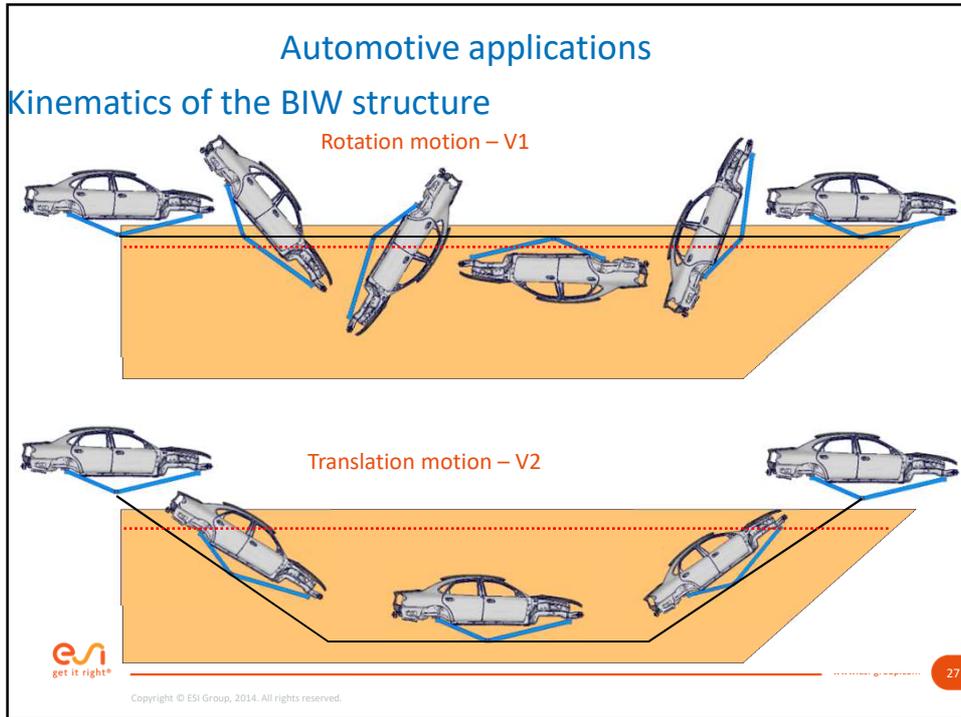
### Automotive applications

Simulation of painting using the SPH elements.  
 Two ways of motion BIW in paint tank (Translation, Rotation).  
 Simulation of BIW kinematics in a paint tank.

- Maximal force and moment in drive engine and joints.
- Flow in BIW structure.



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## Rotating machinery

### Lubrication in gear systems: Industrial need

- Gear systems are key mechanical components used to transmit power.
- Gear systems must be well lubricated
  - Ensure minimal mechanical losses
  - Prevent the rupture of oil film due to accelerated wear.
  - Reduce heat production
- Splash lubrication is a common lubrication method.
- Oil churning is considered as a major source of power loss in gear systems.
- **Industrial need:** Maintain structural integrity of the system with minimal oil volume.
- Problem: splash lubrication properties are hardly predictable.



Planetary gearbox used in wind turbine



Breakage of helical gear due to splash lubrication



Wind energy sector



Aeronautical sector



Automotive industry

There is a need to get reliable insight on the oil churning pattern to drive an optimization process.


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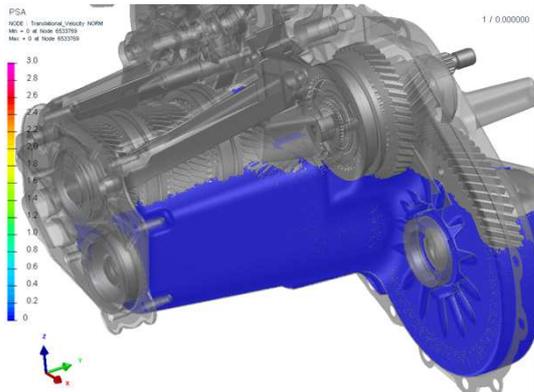
## Rotating machinery

### Lubrication in gear systems: industrial case: 5<sup>th</sup> gear ratio with 2000 rpm

Computing Time

| Simulation conditions  | Numerical value |
|------------------------|-----------------|
| Number of particles    | 500000          |
| Particle diameter (mm) | 1,6             |
| Simulation time (s)    | 2               |
| computing time (days)  | 15              |
| Number of processors   | 12              |

PISA  
MODE : Transitional\_Velocity\_NORM  
Min = 0 at Node 653759  
Max = 3 at Node 653759



Simulation result

1 / 0.000000


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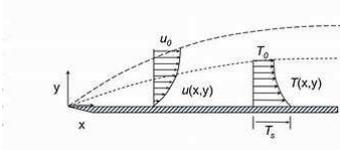
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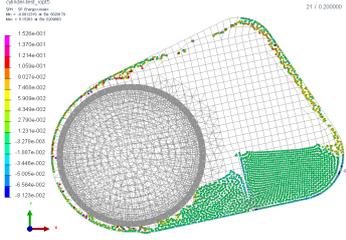
## Rotating machinery

### Lubrication in gear systems: Inclusion of heat transfer

Requirements for SPH software simulation tool:

1. WC-SPH including energy equation
2. Interaction with fast-moving structures
3. Viscosity model (Non-Newtonian, temperature dependent)
4. Heat conduction between particles
5. Heat transport with surface





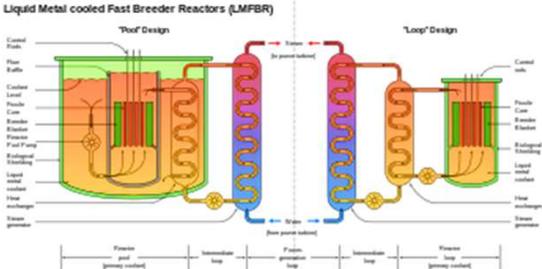
*Particle distribution with the internal energy at 0.2 seconds*

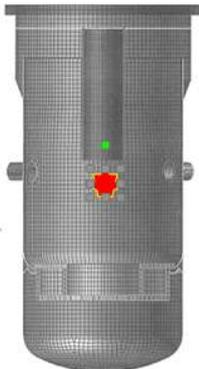

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## Nuclear Reactor Safety

### Hypothetical Core Disruptive Accident in a fast breeder reactor






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### Nuclear Reactor Safety

Highly complex model: geometry, liquid sodium, argon gas, deformable structure, bubble dynamics, leakage

Generation of suitable distribution of (sodium) particles by the EWVT method.

**SPH-FE Analysis of Reactor Safety**

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### Nuclear Reactor Safety

Hypothetical Core Disruptive Accident in a fast breeder reactor

Contour plot of the maximum equivalent plastic strain in the RV structure at the final time of 300 ms.

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### Miscellaneous applications

- Resin molding
- Powder compaction
- Impact on concrete & composites
- Cardiac flow

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### Industrial simulation of fluid flow and fluid-structure interaction with SPH from the VPS software

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